# [Research]

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# Measuring the performance and returns to scale of forest management plans using data envelopment analysis approach (Case study; Iranian Caspian forests)

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### ABSTRACT

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The aim of this study was to assess the relative efficiency of the Iranian forest management plans using the nonparametric method – Data Envelopment Analysis (DEA) as a well-known and robust technique for measuring the relative efficiency of organizations. The relative efficiency of forest management plans was calculated using the most frequency DEA models such as global technical efficiency (CCR), local pure technical efficiency (BCC) and Scale Efficiency (SE) on 12 units in Guilan Province, Iran. According to the results of CCR and BCC models, the efficiency averaged 0.83 and 0.93, respectively. The results of SE discussed a worrying aspect of these units efficiency; namely, there were only 3 efficient forest management plans (Shafaroud, Nav and Fiyab). However, the Scale Efficiency Index (SEI) brings out some interesting points; there were approximately 58% (7 units out of 12) under Increasing Returns to Scale (IRS). Therefore, the managers of forest management plans should focus more on the plans under IRS, so that they will have the opportunity to become more efficient through growth, otherwise managers will not be able to promote their overall productivity.

Key words: Data envelopment analysis; Measuring the performance; Returns to scale; Forest management plans.

#### INTRODUCTION

Efficiency and productivity measurement in organizations has received a great deal of attention both in research and in practice. It means that determining the efficiency has become increasingly important in many areas of human activity. In forestry, the determination of efficiency of forest plans is management very complicated multiple of because of goals forest management, i.e. in the last few decades, forest management has been focused on multifunction usage (economic, ecological and social functions) and general benefits of forests. Owing to the multiple benefits and advantages offered by the forest as well as the non-market nature of part of these outputs, measuring the efficiency in forestry is highly demanding (Sporcic et al. 2009). Approach to this problem is particularly interesting when there are no clear success parameters, and when the efficiency of using several different resources/inputs is measured for achieving several different outputs. A well-documented method in the operations research is Data Envelopment Analysis (DEA) that was originally introduced by Charnes et al. (1978) in the form of mathematical programming, based on an earlier work of Farrell (1957). Afterwards, In the DEA literature, many authors have extended techniques to measure the relative performances of operational units in different conditions. DEA utilizes linear programming (LP) to evaluate the relative performance of a set of homogeneous decision making units (DMUs) with multiple

incommensurate inputs and outputs without requiring a specified functional form.

The LP can be formulated in many ways and is a transformation of the original fractional programming problem, see section 2.1.2: Output Maximization and Input Minimization DEA Programs on page 42 of Ramanathan as section Data (2003)as well 2.5: Envelopment Analysis on page 29 of Subhash (2004). Indeed, attempts to understand the relationship between the technology of a DMU, its efficiency and environment, and the measurement of Returns to Scale (RTS) are not new to DEA. But one of the key properties of the production structure is the scale of operations.

It receives particular interest because the existence of economies or diseconomies of scale may have different implications for the market structure and conduct. Hence, the economic concept of RTS has also been widely studied within the framework of DEA to answer a critical quest in any study of productive efficiency; whether the underlying technology exhibits increasing, constant, or decreasing returns to scale. The economic concept of RTS is extremely important in forestry as well, because forests are rare also have recourses and multifunction (marketable and non-marketable) uses in which monitored by forest management plans. So, in a rational insight, assessing the performance of these plans to propose appropriate solutions for improving their performance and scale efficiency state is really vital.

In general, two main categories have been followed for treating RTS in DEA: first, RTS measurement using BCC-DEA models; this type of research efforts includes Banker & Thrall (1992), Tone (1996), Golany & Yu (1997), Sueyoshi (1999), Cooper *et al.* (2000), Tone & Sahoo (2003); the second, RTS measurement developed by Färe, Grosskopf & Lovell (FGL-DEA model) who used a quantitative measurement of scale elasticity. In fact, this type of research can be traced to the efforts of Färe *et al.* (1983, 1985, and 1994). Noteworthy, the alternative measurements provided by the FGL-DEA approach is an important one because this approach identifies RTS through the ratios of a series of relative efficiencies obtained from different DEA models with radial measure, which has different constraints (Färe et al. (1983). These ratios are developed from the model pairs that differ only in conditions of the convexity and sub-convexity that are satisfied (Banker et al. 2004). Despite that DEA has been applied in a wide range of applications, there are few studies in forestry by this non-parametric approach. For instance, Kao & Yang (1992) used the DEA efficiency results to appraise three alternatives proposed bv Taiwan Forestry Bureau the for reorganizing the 13 forest districts considered in their earlier study (Kao & Yang 1991). The efficiency of 19 public Forestry Boards in Finland was evaluated using DEA (Viitala & Hanninen 1998).

The efficiency of the Croatian forestry organization was evaluated by non-parametric models (Sporcic *et al.* 2009), their research revealed DEA as a powerful multi criteria decision making tool for support in forest management. The DEA model was used to measure the productive efficiency of forest enterprises in the Mediterranean Region of Turkey (Korkmaz 2011).

DEA was first used to assess the efficiency of Iranian forest industries by Mohammadi Limaei (2013). He investigated the efficiency of 14 Iranian forest companies and forest management in 2010. Efficiency of the companies was estimated using a traditional DEA model and a two-stage DEA model.

Therefore, due to the important role of forests (economic, include multiple usage to ecological and social functions) this study is conducted to estimate the relative efficiency to scale of some forest and returns management plans in the north of Iran to disseminate the necessary information for manager of forest management plans until they will be able to adjust the units operating scale and become more efficient through

growth. The DEA method is, therefore, well suited to be used in this case study.

#### MATERIALS AND METHODS DEA models

Conventionality DEA is defined as a linear programming methodology (Lin & Wang 2014) which allows to assess the performance of multiple DMUs when the production process presents a structure of multiple inputs and outputs (Tone & Tsutsui 2014; Oral *et al.* 2014). In this matter, there are many DEA models with their pros and cons, thus, with respect to this paper goals, the most frequently applied DEA model is used as follows.

#### CCR model

Charnes *et al.* (1987) formulated a DEA model, referred to as CCR [Charnes, Cooper & Rhodes], with Constant Returns to Scale (CRS) assumption (Model 1). A CRS assumption implies that all DMUs would be able to increase their output by a similar proportion, given an increase in the rate of their inputs, no matter what their scales are. The efficiency score resulting from a CCR model is called the global technical efficiency.

 $\begin{bmatrix} CCR \end{bmatrix} \quad \min y_0 = \theta - \varepsilon \left( \sum_{r=1}^{s} \sum_{r=1}^{s} \sum_{i=1}^{m} \sum_{i=1}^{m} \right)$ st:

$$\sum_{j=1}^{n} y_{rj} \lambda_{j} - \sum_{r}^{+} = y_{r0} \qquad (r = 1, 2, ..., s)$$

$$\sum_{j=1}^{n} x_{ij} \lambda_{j} + \sum_{i}^{-} = \Theta x_{i0} \qquad (i = 1, 2, ..., m)$$

$$\lambda_{j}, \sum_{r}^{+}, \sum_{i}^{-} \ge 0 \quad \forall i, j, r \qquad (j = 1, 2, ..., n)$$
(1)

where:  $x_{ij}$  = amount of input i used by unit j,

 $y_{rj}$  = amount of output r is produced by unit j,

 $\mathcal{E}$  = a small non-Archimedean quantity which prohibits any inputs/outputs factor to be ignored.

Due to the input-oriented nature of this model, the objective function tries to reduce input amounts ( $\theta$ ) by fixing output levels. In fact,  $\theta$  is a real decision variable and  $\lambda$  is a nonnegative vector of decision variable that in this sample to choose each allowable vector ( $\lambda$ j) for making an upper limit for outputs and a lower limit for inputs of DMU0. Hence the optimal  $\theta$ , denoted by  $\theta^*$ , is not greater than 1 (Cooper *et al.* 2007).

Definition 1.A decision maker is fully efficient if and only if both  $\theta^* = 1$  (optimal solution problem) and  $s_r^{+} = s_i^{-} = 0$  (slack input and output variables).

#### BCC model

The CCR model (Model 1) can be modified to accommodate Variable Returns to Scale (VRS). This model was introduced by (Banker et al. 1984), referred to as BCC, and requires a convexity constraint (2) added to the CCR model (1). Noteworthy, the convexity of the production possibility set is a maintained hypothesis in DEA because the convexity ensures that when two or more input-output combinations are known to be feasible, any weighted average of the input bundles can produce a similarly weighted average of the corresponding output bundles (Subhash 2004). Therefore, in this model, each DMU against other DMUs in the same scale range as well as the efficiency score provided by a BCC model is called local pure technical efficiency.

$$\sum_{j=1}^{n} \lambda_{j} = 1 \qquad (j = 1, 2, ..., n)$$
(2)

Definition 2. The definition of efficient decision maker is the same as definition 1.

#### SE model

The scale efficiency (SE) of a DMU can be calculated based on its global technical efficiency and local pure technical efficiency resulting from CCR and BCC models, respectively (3). SE represents the inefficiency of a DMU which is merely due to its scale of operations. This model can be formulated in the following form (Cooper *et al.* 2007).

Definition 3. A decision maker is fully efficient if and only if both  $\theta^* = 1$  (optimal solution problem).

$$SE = \frac{\theta_{CCR}^*}{\theta_{BCC}^*} \tag{3}$$

#### SEI/ FGL model

Färe et al. (1985) introduced the following "scale efficiency index" (SEI) method or FGL model, which is based on Non-Increasing Returns to Scale (NIRS), to determine the nature of local RTS for  $DMU_o$  (Tone & Sahoo, 2005):

 $[SEI / FGL] \quad \min y_0 = \theta - \varepsilon \left( \sum_{r=1}^{s} \sum_{r=1}^{+} \sum_{i=1}^{m} \sum_{i=1}^{-} \right)$ 

st:

$$\sum_{j=1}^{n} y_{ij}\lambda_{j} - \stackrel{+}{}_{r}^{=} y_{r0} \qquad (r = 1, 2, ..., s)$$

$$\sum_{j=1}^{n} x_{ij}\lambda_{j} + \stackrel{-}{s}_{i}^{=} = \theta x_{i0} \qquad (i = 1, 2, ..., m)$$

$$\sum_{j=1}^{n} \lambda_{j} \leq 1 \qquad (j = 1, 2, ..., m)$$

$$\lambda_{j}, \stackrel{+}{s}, \stackrel{-}{s} \geq 0 \quad \forall i, j, r$$

$$(1)$$

(4)

In fact, they proposed a method by changing  $\sum_{j=1}^{n} \lambda_j = 1$  from (Model 2) to  $\sum_{j=1}^{n} \lambda_j \leq 1$  (Model 4) and these following steps:

If  $\theta_{CCR}^* = \theta_{BCC}^*$ , then DMU<sub>o</sub> exhibits CRS

and also is fully efficient by SE; otherwise if  $\theta^*_{CCR} < \theta^*_{BCC}$ , then DMU<sub>o</sub> exhibits IRS if  $\theta^*_{SEI} < \theta^*_{BCC}$ , and DMU<sub>o</sub> exhibits NIRS if  $\theta^*_{SEI} = \theta^*_{BCC}$ .

#### Case study

The area of natural forest in Iran is approximately 12.4 million hectares, equal to 7.5% of the total area of Iran. Of this, approximately 1.9 million hectares are commercial forests called Iranian Caspian, Hyrcanian or Northern forests which is controlled by forest management plans.

In this research, according to forestry experts' idea, two inputs (plantation cost and stock before executing the forest management plan,

called stock 1) and two outputs (harvesting revenue and stock after executing the plan, called stock 2) were considered. At least 12 forest management plans had to select using rule of thumb in DEA approach. Hence, the number of DMU should follow:

 $n \ge \max\{m \times s, 3(m+s)\}$ 

where n = number of DMUs, m = number of inputs, and s = number of outputs. Afterwards, we assume that this (or other) degrees of freedom conditions are satisfied and that there is no trouble from this quarter (Cooper *et al.* 2011). It should be noted that the length of the planning horizon includes 10 years. Hence, in this case, the average data of a ten-year period were considered. Moreover, the monetary data were adjusted by the Consumer Price Index (CPI) of Iran in the base year 2011 (Table 1).

#### RESULTS

The results of global technical efficiency (CCR) and local pure technical efficiency (BCC) are meaningfully different; the number of efficient units by CCR is 3 and by BCC is 6 and also the efficiency averages for CCR and BCC are 0.83 and 0.93, respectively (Table 2). The results of BCC and FGL models indicate that most of forest management plans 58% (7 out of 12) are under IRS.

Also, this comparative approach shows that two forest management plans are under NIRS and the rest of them are under CRS as well as they are fully efficient (score 1) by SE model (Table 3).

The results of the scale efficiency (SE) model show the distance between the boundary fixed and variable returns to scale (CCR and BCC) in which based on this model there is a considerable distance between them, i.e. there are only 3 (Shafaroud, Nav and Fiyab) efficient forest management plans (Fig. 1).



Forest management plans

Fig. 1. The result of SE model.

Table 1. Mean values of input and output data of forest management plans used in DEA models.

	Input		Output		
- Forest management	Plantation cost (Iranian	Stock 1	Harvesting	Stock 2	
nlang	million Rials)	(m <sup>3</sup> .ha <sup>-1</sup> )	revenue	(m <sup>3</sup> .ha <sup>-1</sup> )	
plans		(Iranian million			
			Rials)		
Shafaroud	53.07177	210.52	14173.86	226.46	
Nav	254.2138	219.62	104653.89	254.12	
Chojeye	236.1694	231.77	22571.13	226.59	
Liyashi Sara	387.4239	241.558	50075.23	250.06	
Changol	514.7962	197.516	33551.23	214.75	
Fiyab	95.52919	236.904	49391.76	319.84	
Siyahroud	249.4373	255.86	39079.87	254.06	
Poya Sepidar1	135.333	289.45	53353.27	358.97	
Poya Sepidar2	318.9613	208.93	34815.33	174.21	
Narmash	148.601	193.77	22207.49	218.42	
Narvan	189.1934	180.5	37928.82	210.3	
Lael	361.6372	159.67	32885.47	138.71	

In this study, GAMS software was used for model analyses.

Tał	ole 2.	Results o	of C	CR	and	BCC	mod	els.
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Forest management plans	CCR	BCC
Shafaroud	1	1
Nav	1	1
Chojeye	0.72	0.81
Liyashi Sara	0.79	0.84
Changol	0.81	0.93
Fiyab	1	1
Siyahroud	0.74	0.79
Poya Sepidar1	0.92	1
Poya Sepidar2	0.64	0.82
Narmash	0.83	0.99
Narvan	0.88	1
Lael	0.68	1

Forest management plans	BCC	SEI/FGL	RTS
Shafaroud	1	1	Consistent*
Nav	1	1	Consistent*
Chojeye	0.81	0.72	Increasing
Liyashi Sara	0.84	0.79	Increasing
Changol	0.93	0.81	Increasing
Fiyab	1	1	Consistent*
Siyahroud	0.79	0.79	Non-increasing
Poya Sepidar1	1	1	Non-increasing
Poya Sepidar2	0.82	0.64	Increasing
Narmash	0.99	0.83	Increasing
Narvan	1	0.88	Increasing
Lael	1	0.68	Increasing

\* Under CRS and also fully efficient by SE model.

#### DISCUSSION

To provide a preliminary picture of Iranian forest management plans performance and returns to scale, fundamental analyses were performed using different DEA models. In this study the input- oriented DEA models are used for efficiency evaluation because the DMUs can be optimized using their proper inputs. The CCR and BCC input-oriented models with fixed and variable returns to scale were used for measuring the global technical efficiency and local pure technical efficiency respectively. The results are summarized in Table 2. As shown in the Table, the efficiency averaged 0.83 and the number of efficient units was 3 by CCR model, while the efficiency averaged 0.93 and the number of efficient units was 6 by BCC model. These differences may be due to the features of returns to scale in these two models. In constant returns to scale method or CCR, a small unit, regardless to its optimum scale, is compared to the other units which could be higher than it. Consequently, the small units get a lower efficiency score than the other units. In variable returns to scale method or BCC, each unit is compared with the same optimum scale units. Consequently, the number of efficient units by CCR is less than BCC approach. These results are in line with those obtained by Kao (2000); Nvrud & Baardsen (2003); Diaz-Balteiro et al. (2006); Sporcic et al. (2009), who obtained similar logical consequences. The SE is calculated

from the results of the CCR and BCC; based on model 3. The results of this approach are shown in Fig. 1 exhibiting that the SE of forest management plans is quite low, i.e. there are only 3 (out of 12) efficient forest management plans in which the distance between CCR and BCC is found to be considerable. In addition, SE less than 1 for the other plans indicates that the overall efficiency may be improved by changing the practical scale. These noticeable remarks pointed out in similar previous studies (Vahid & Sowlati 2007; Zadmirzaei et al. 2015) on forest industries. On the contrary, the SE cannot determine the elasticity of scale efficiency or RTS; when VRS are considered, the technical efficiency indices are greater than, or equal to, the efficiencies under constant returns to scale (CRS). A technically efficient DMU may be operating at increasing (IRS) or non-increasing (NIRS) returns to scale. Thus, to closer this gap, SEI/FGL-DEA model is used (model 4). The results of RTS are shown in Table 3 where there is a comparison between BCC and SEI model. As it can be observed. based on this comparative approach, most of the forest management plans 58% (7 out of 12) are under IRS. Also two plans are under NIRS and the rest of them are under CRS as well as they are fully efficient (score 1) by SE model. In like manner Salehirad & Sowlati (2007) and also Gaspar et al. (2009) using RTS models figured out that the adjustment of firms to their optimal size is

slow due to their particular. Inputs, introducing a new complication, as firms cannot choose the optimal level of any inputs instantaneously. Consequently, scale measures must account for this fact. So, obviously, the interpretation of the RTS brings out some interesting points to determine the elasticity of scale efficiency to apply whole capacities of production units.

#### CONCLUSION

Measuring the relative efficiency of forest management plans has allowed us to determine their average levels of technical efficiency, and to identify the RTS that could permit them to denote the elasticity of scale efficiency for improving their current level of efficiency or reduce their inefficiencies. To sum up, with respect to obtained efficiency scores from CCR and BCC models it can be proclaimed that the investigated forest management plans generally give us fine performances. It means that these fully efficient plans reduce their inputs consumption, while keep a constant output and consequently level increase their efficiency and profitability. However, the results of the SE model discuss a worrying aspect of plans efficiency in which there was a considerable distance between these plans optimum operating scales (only 3 efficient plans out of 12). But the quest for economies of scale is more interesting to determine whether the scale inefficiencies are because the plans are producing at below or above the optimal level. With this intention, the SEI/FGL-DEA model brings out some interesting points; forest management plans under CRS are completely efficient in operating scales, i.e. these plans use all capacities of their optimum operational scale to generate more revenues and make sound business sense. The forest management plans under IRS would be attractive acquisition targets because they have the opportunity to become more efficient through growth. On the other hand, forest management plans under NIRS are

unattractive merger/acquisition targets since they are already "too large". In conclusion, the managers of forest management plans should more focus on plans under IRS (approximately 58% of the investigated forest management plans) until they will be attained the optimum operational scale. Otherwise managers will not be able to promote their overall productivity. Therefore, the main contribution of this study is accepted by results of this work: to disseminate the necessary information for manager of forest management plans until they will be able to adjust the units operating scale and become more efficient through growth.

#### Limitation and future research directions

It should be noted that the limitations of the study can be defined with respect to the dataset and DEA models. In relation to the dataset, depending on data accessibility, we may also consider some other variables such as plantation costs, harvesting costs, road construction costs, forest tending costs, economic values of the stock 2, etc. Finally, although some factors that could have affected the performance were discussed here, more comprehensive research is required to fully explain performance variations of the forest management plans. For instance, if there are large price variations, it is rational to adapt harvesting to prices. In such cases, it is important to have flexible systems with some extra harvesting capacity which can be employed when prices are very good. In contrast, when prices are not very good, it does not prefer to harvest at full capacity utilization (see also Lohmander et al. 2008; Mohammadi Limaei et al. 2010).

Therefore, as future research avenues, it is recommended that the other researchers consider the multidimensional economic database as input and output variables on application of DEA in forest management contexts because of multifunction usage (economic, ecological and social functions) of forests.

#### REFERENCES

- Banker, RD, Charnes, A & Cooper, WW 1984, some models for estimating technical and scale inefficiencies in data envelopment analysis. *Management Science*, 30: 1078-1092.
- Banker, RD & Thrall, RM 1992, Estimation of returns to scale using data envelopment analysis. European Journal of Operational Research, 62: 74–84.
- Banker, RD, Cooper, WW, Seiford, LM, Thrall, RM & Zhu, J 2004, Returns to scale in different DEA models. *European Journal of Operational Research*, 154: 345–362.
- Charnes, A, Cooper, WW & Rhodes, E 1978, Measuring the efficiency of decisionmaking units. *European Journal of Operational Research*, 2: 429–444.
- Cooper, WW, Seiford, LM & Tone, K 2000, Data envelopment analysis: A comprehensive text with models, applications, references and DEA-solver software. Boston: Kluwer Academic Publishers, p. 318.
- Cooper, WW, Seiford, LM & Tone, K 2007, Data Envelopment Analysis: A comprehensive text with models, applications, references and DEA-Solver Software. 2<sup>nd</sup> Ed. Springer US, Springer-Verlag, US, p. 492.
- Cooper, WW, Seiford, LM & Zhu, J 2011, Handbook on Data Envelopment Analysis. 2<sup>nd</sup> Ed. Springer US, Springer Science + Business Media, LLC. p. 498.
- Diaz-Balteiro, I, Herruzo, A, Martinez, M & Gonzalez-Pachon, J 2006, An analysis of productive efficiency and innovation activity using DEA: An application to Spain's wood-based industry. *Forest Policy and Economics*, 8: 762–773.
- Farrell, MJ 1957, The measurement of productive efficiency. *Journal of the Royal Statistical Society*, 120: 253–282.
- Färe, R, Grosskopf, S & Lovell, CAK 1983, The structure of technical efficiency. *Scandinavian Journal of Economics*, 85: 181-190.
- Färe, R, Grosskopf, S & Lovell, CAK 1985, *The measurement of efficiency of production*. Kluwer Nijhoff, Boston, p. 216.

- Färe, R, Grosskopf, S & Lovell, CAK 1994, *Production frontiers*. Cambridge University Press, p. 296.
- Gaspar, P, Mesías, FJ, Escribano, M & Pulido, F 2009, Assessing the technical efficiency of extensive livestock farming systems in Extremadura, Spain. *Livestock Science*, 121:7–14.
- Golany, B & Yu, G 1997, Estimating returns to scale in DEA. *European Journal of Operational Research*, 103: 28-37.
- Kao, C & Yang, Y 1991, Measuring the efficiency of forest management. *Forest Science*, 37: 1239-1252.
- Kao, C & Yang, Y 1992, Reorganization of forest districts via efficiency measurement. *European Journal of Operational Research*, 58: 356-362.
- Kao, C 2000, Measuring the performance improvement of Taiwan forests after reorganization. *Forest Science*, 46: 577-584.
- Korkmaz, M 2011, Measuring the productive efficiency of forest enterprises in Mediterranean region of Turkey using data envelopment analysis. *African Journal* of *Agricultural Research*, 6: 4522-4532.
- Lin, B & Wang, X 2014, Exploring energy efficiency in China's iron and steel industry: A stochastic frontier approach. *Energy Policy*, 72: 87-96.
- Lohmander, P & Mohammadi Limaei, S 2008, Optimal continuous cover forest management in an uneven-aged forest in the North of Iran. *Journal of Applied Sciences*, 8: 1995-2007.
- Mohammadi Limaei, S, Lohmander, P & Obersteiner, M 2010, Decision making in forest management with consideration of stochastic prices. *Iranian Journal of Operations Research*, 12: 32-40.
- Mohammadi Limaei, S 2013, Efficiency of Iranian forest industry based on DEA models. *Journal of Forestry Research*, 24: 759-765.
- Nyrud, AQ & Baardsen, S 2003, Production Efficiency and Productivity Growth in Norwegian Sawmilling. *Scandinavian Journal of Forest Research*, 49: 89-97.

- Oral, M, Oukil, A, Malouin, JL & Kettani, O 2014, The appreciative democratic voice of DEA: A case of faculty academic performance evaluation. *Socio-Economic Planning Sciences*, 48: 20-28.
- Ramanathan, R 2003, An introduction to data envelopment analysis: A tool for performance measurement. Sage Publications India, p. 202.
- Salehirad, N & Sowlati, T 2007, Dynamic efficiency analysis of primary wood producers in British Columbia. *Mathematical and Computer Modelling*, 45: 1179–1188.
- Sporcic, M, Martinic, I, Landekic, M & Lovric, M 2009, Measuring efficiency of organizational units in forestry by Nonparametric model. *Croatian Journal of Forest Engineering*, 30: 1-13.
- Subhash, CR 2004, Data Envelopment Analysis: Theory and techniques for economics and operations research. Cambridge University Press, p. 366.
- Sueyoshi, T 1999, DEA duality on returns to scale (RTS) in production and cost analyses: an occurrence of multiple solutions and differences between production-based and cost-based RTS estimates. *Management Science*, 45: 1593– 1608.
- Tone, K 1996, A simple characterization of returns to scale in DEA. *Journal of the*

*Operations Research Society of Japan,* 39: 604-613.

- Tone, K & Sahoo, BK 2003, Scale, indivisibilities and production function in Data Envelopment Analysis. *International Journal of Production Economics*, 89: 165-195.
- Tone, K & Sahoo, BK 2005, Evaluating cost efficiency and returns to scale in the life insurance corporation of India using data envelopment analysis. *Socio-Economic Planning Sciences*, 39: 261–285.
- Tone, K & Tsutsui, M 2014, Dynamic DEA with network structure: A slacks-based measure approach. *Omega*, 42: 124-131.
- Vahid, S & Sowlati, T 2007, Efficiency analysis of the Canadian wood-product manufacturing subsectors: A DEA approach. *Forest Products Journal*, 57: 71-77.
- Viitala, EJ & Janninen, H 1998, Measuring the efficiency of public forestry organizations. *Forest Science*, 44: 298-307.
- Zadmirzaei, M, Mohammadi limaei, S & Amirteimoori, A 2015, Efficiency analysis of paper mill using data envelopment analysis models (Case study: Mazandaran Wood and Paper Company in Iran). Journal of Agriculture Science and Technology, 17: 1381-1391.

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# چکیدہ

هدف از تحقیق مذکور ارزیابی کارایی نسبی طرحهای جنگلداری ایران با استفاه از روش ناپارامتریک تحلیل پوششی دادهها (DEA) است. برای این منظور، از DEA بعنوان روش شناخته شده و قدر تمند جهت اندازه گیری کارایی نسبی سازمان ها (DEA) استفاده گردید. کارایی نسبی ۲۱ طرح جنگلداری در استان گیلان با استفاده از مدلهای رایج DEA از قبیل کاریی فنی جهانی (CCR)، کارایی نسبی ۲۱ طرح جنگلداری در استان گیلان با استفاده از مدلهای رایج DEA از قبیل کاریی فنی حهانی (CCR)، کارایی نسبی محلی (SE) و کارایی مقیاس (SE) محاسبه گردید. مطابق نتایج مدل های CCR و PA، و BCC)، و کارایی مقیاس (SE) محاسبه گردید. مطابق نتایج مدل های CCR و GCC، میانگین کارایی بتر تیب ۲۸۳ و PA، بوده است. نتایج SE تصویر نگران کننده ای را در خصوص کارایی واحدهای تحت ارزیابی بیان داشت، بدین معنی که تنها ۳ طرح جنگلداری (شفارود، ناو و فیاب) کارا اعلام گردیدند. اما بکارگیری شاخص کارایی مقیاس (SE) نکات قابل توجه ای را در این خصوص بیان داشت، بطوریکه تقریبا ۵۸٪ (۲ از ۲۱واحد تحت تسخص کارایی مقیاس (SE) و کارایی میان داشت، بطوریکه تقریبا ۵۸٪ و ۲۹(ی در این خصوص بیان داشت، بطوریکه تقریبا ۵۵٪ (۲) از ۲۱واحد تحت ارزیابی میان داشت، بدین معنی که تنها ۳ طرح جنگلداری (شفارود، ناو و فیاب) کارا اعلام گردیدند. اما بکارگیری شاخص کارایی مقیاس (SE) نکات قابل توجه ای را در این خصوص بیان داشت، بطوریکه تقریبا ۵۸٪ (۲ از ۲۱واحد تحت ارزیابی) در ناحیه بازه به مقیاس افزایشی تولید (IRS) قرار داشتند. بنابراین، مدیران طرحهای جنگلداری می بایست برای افزایش کارایی بیشترین تمرکز خود را بر روی طرحها در ناحیه IRS قرار دهند، در غیر این صورت قادر به افزایش بهرموری لخوا می کاری خود را بر روی طرحها در ناحیه IRS قرار دهند، در غیر این صورت قادر به افزایش بهرموری افزایش بهرموری کری و در ایر داشتند. بنابراین، مدیران طرحهای جای در افزایش بهرموری افزایش بهرموری در افزایش بهرموری در مای کاری بی خواهند بود. در فیر این صورت قادر به افزایش بهرموری در افزایش بهرموری

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